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Metaphor and Abduction

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None but a geometrician or a blockhead can talk without a metaphor.

Jean-Jacques Rousseau,

Julie, or La Nouvelle Héloise

Abstract

In this paper a recent approach to inference in text understanding based on abduction is applied to the problem of metaphor interpretation. The fundamental ideas in the "interpretation as abduction" approach are outlined. A succinct characterization of interpretation is given, along with a brief example and a description of the principal features of a weighted abduction scheme that is used. This approach is shown to lead to an elegant integration of syntax, semantics, and pragmatics. Three examples of metaphor interpretation are then analyzed within the abductive framework to determine what problems arise. The examples are a conventionalized metaphor schema, a standard category metaphor contextually interpreted, and a novel metaphor. The primary problem that arises for metaphor interpretation in the abductive framework is dealing with the fact that metaphors are not literally true. Two perspectives on this difficulty are offered.

1 Introduction

The use of inference in text understanding has been an important theme in computational linguistics for at least two decades, and there have been a number of inference-based approaches to metaphor interpretation (e.g., Carbonell, 1982; Hobbs, 1983; Indurkhya, 1987). In recent years, a particularly elegant formulation of the use of inference in text understanding has emerged, based on abduction, or inference to the best explanation (e.g.,

Charniak and Goldman, 1988; Hobbs et al., 1988, 1990; Norvig, 1987). A great many problems in interpretation, such as reference resolution, expansion of metonymies, and resolution of some lexical and syntactic ambiguities, have been shown to be subsumed under this new approach. This paper is an attempt to extend the abductive approach to cover metaphor interpretation as well, by recasting an inference-based approach to metaphor in light of one of the abductive frameworks. Such an effort ought to have the highest priority for any new approach to interpretation because, as Rousseau and many others since have pointed out, metaphor pervades discourse.

In Section 2 some basic assumptions about knowledge representation are laid out.

In Section 3 the fundamental ideas in the "interpretation as abduction" approach are outlined, though necessarily briefly. A succinct characterization of interpretation is given, along with a brief example. The principal features of a weighted abduction scheme are described and shown to lead to an elegant integration of syntax, semantics, and pragmatics.

In Section 4 three examples, analyzed in an older framework in Hobbs (1983), are reanalyzed within the abductive framework to determine what problems arise. The examples are a conventionalized metaphor schema, a standard category metaphor contextually interpreted, and a novel metaphor.

The primary problem that arises for metaphor interpretation in the abductive framework is dealing with the fact that metaphors are not literally true. In Section 5 two perspectives on this difficulty are offered.

2 Representation

In this paper formal logic is the representation language. This choice ought to be uncontroversial. There are six features any adequate representation language ought to have. Five of them are just the features that the syntax of formal logic provides. The sixth is a feature that many researchers working in a logical framework are attempting to provide. All but one of these is provided by neural nets as well, indicating that there is in fact agreement about requirements across a broad range of representational positions.¹

¹Neural nets are of course a computational device and not, strictly speaking, a representation language. However, the mode of computation they provide can be thought of as an inference mechanism. In many of their uses, the nodes are given propositional interpretations, and even in cases where their behavior is learned rather than programmed, intellectual curiosity often leads one to ask for a propositional characterization of what contribution to the total behavior of the system each node makes.

- 1. Conjunction: There needs to be a way for two propositions to have an additive effect. Conjunction provides this in formal logic. The additive effect of excitatory links provides this in neural nets.
- 2. Implication and Modus Ponens: One needs implicative rules, that allow one proposition to be concluded from another. Implication and modus ponens provide this in formal logic. In neural nets, the excitatory links between nodes provide it. Thus, when one node is activated, it will, under the right circumstances, cause other nodes to which it is connected to be activated as well.
- 3. Negation and Recognizing "Obvious" Contraditions: There needs to be a way of recognizing at least the most obvious contradictions, such as that a cat is not a dog. This is provided by negation in formal logic. It is provided by inhibitory links in neural nets.
- 4. Predicate-Argument Relations: There must be a way of expressing relations among entities, and of distinguishing which entity plays what role in the relation. This capability is provided in first-order predicate calculus. It is one of the principal features that frame-like representations seek to provide. Predicate-argument relations can be represented in neural nets without difficulty.
- 5. Variables and Universal Instantiation: Variables are required in some form or other, in order to express general knowledge, and there must be a way of binding variables to particular values. Formal logic provides a particularly clean way of doing this. Neural nets do not, and this is generally recognized as perhaps the greatest shortcoming of neural nets as a computational framework for simulating intelligent behavior.

There are some who would claim that, rather than using general knowledge, we understand new situations using previously acquired particular knowledge by a process of analogy or reminding. But in every analogy there is an implicit generalization, whether or not we acknowledge it explicitly. Thus, suppose we know about an old situation the following facts:

$$p_1(A), p_2(A), p_3(A), p_4(A), p_5(A), q(A)$$

Then we encounter a new situation in which the following are true:

$$p_1(B), p_2(B), p_4(B)$$

We hypothesize, by analogy, that q(B) is also true. But this corresponds to using the implicit generalization

$$(\forall x)p_1(x) \wedge p_2(x) \wedge p_4(x) \supset q(x)$$

Such generalizations can be made defeasible in a number of ways, including using "et cetera" predications in an abductive framework, as described in Section 3.3.

6. "Soft Corners": There must be ways in which some inferences can be favored over others. There must be ways to accommodate inconsistent propositions. This is one of the primary strengths of neural net representations. Researchers working on model preference semantics for nonmonotonic logics and researchers working on probabilistic reasoning are searching for the appropriate means to give hard-edged logic softer corners. The scheme for weighted abduction presented here is another attempt to do just that.

Any system with these features can be used in three different ways—deductive-ly, inductively, and abductively. In deduction, from $(\forall x)p(x) \supset q(x)$ and p(A), one concludes q(A). In induction, from p(A) and q(A), or more likely, from a number of instances of p(A) and q(A), one concludes $(\forall x)p(x) \supset q(x)$. Abduction is the third possibility; from $(\forall x)p(x) \supset q(x)$ and q(A), one concludes p(A). One can think of q(A) as the observable evidence, of $(\forall x)p(x) \supset q(x)$ as a general principle that could explain q(A)'s occurrence, and of p(A) as the inferred, underlying cause or explanation of q(A). Of course, this mode of inference is not valid; there may be many possible such p(A)'s. Other criteria of cost and utility are needed to choose among the possibilities.

In this paper we will use formal logic as our representation language, and we will use it abductively as our tool for interpreting natural language discourse.

3 Interpretation as Abduction

3.1 Characterizing Interpretation

Abductive inference is inference to the best explanation. The process of interpreting sentences in discourse can be viewed as the process of providing the best explanation of why the sentences would be true. More precisely, the process of interpreting a sentence can be described as follows:

To interpret a sentence:

Prove the logical form of the sentence,
 together with the constraints that predicates impose on
 their arguments,
 allowing for coercions,
 Merging redundancies where possible,
 Making assumptions where necessary.

By the first line we mean "prove from the predicate calculus axioms in the knowledge base, the logical form that has been produced by syntactic analysis and semantic translation of the sentence." By "coercion" we mean the function or relation that maps from the explicit argument to the intended implicit argument in cases of metonymy, such as the mapping from "Shake-speare" to "the plays of Shakespeare" in the interpretation of the sentence "I like to read Shakespeare."

In a discourse situation, the speaker and hearer both have sets of private beliefs, and there is a large overlapping set of mutual beliefs. An utterance spans the boundary between mutual belief and the speaker's private beliefs. It is a bid to extend the area of mutual belief to include some private beliefs of the speaker's.² It is anchored referentially in mutual belief, and when we prove the logical form and the constraints, we are recognizing this referential anchor. This is the given information, the definite, the presupposed. Where it is necessary to make assumptions, the information comes from the speaker's private beliefs, and hence is the new information, the indefinite, the asserted. Merging redundancies is a way of getting a minimal, and thus a best, interpretation.

This approach to discourse interpretation has been implemented in the TACITUS system (Hobbs et al., 1990) at SRI International, using Stickel's Prolog Technology Theorem Prover (Stickel, 1989). The system has been employed in several moderate-scale applications.

John called the Boston office. Did John call the Boston office? John, call the Boston office.

is the same.

²This is clearest in the case of assertions. But questions and commands can also be conceived of as primarily conveying information—about the speaker's wishes. In any case, most of what is required to interpret the three sentences,

3.2 An Example

This characterization, elegant though it may be, would be of no interest if it did not lead to the solution of the discourse problems we need to have solved. A brief example will illustrate that it indeed does.

But first a notational convention that is used throughout this paper: we will take p(x) to mean that p is true of x, and p'(e,x) to mean that e is the eventuality or possible situation of p being true of x. This eventuality may or may not exist in the real world. The unprimed and primed predicates are related by the axiom schema

$$(\forall x)p(x) \equiv (\exists e)p'(e,x) \land Rexists(e)$$

where Rexists(e) says that the eventuality e does in fact really exist. This notation, by reifying events and conditions, provides a way of specifying higher-order properties in first-order logic. This Davidsonian reification of eventualities (Davidson, 1967) is a common device in AI. See Hobbs (1985) for further explanation of the specific notation and ontological assumptions.

The example is

The Boston office called.

This example illustrates three problems in "local pragmatics", the reference problem (What does "the Boston office" refer to?), the compound nominal interpretation problem (What is the implicit relation between Boston and the office?), and the metonymy problem (How can we coerce from the office to the person at the office who did the calling?).

Let us put these problems aside and interpret the sentence according to characterization (1). Ignoring tense, the logical form is something like

(3)
$$(\exists e, x, o, b) call'(e, x) \land person(x) \land rel(x, o)$$

 $\land office(o) \land nn(b, o) \land Boston(b)$

That is, there is a calling event e by a person x related somehow (possibly by identity) to the explicit subject of the sentence o, which is an office and bears some unspecified relation nn to b which is Boston. The requirement that x be a person is the constraint that the predicate call' imposes on its agent argument.

Suppose our knowledge base consists of the following facts: We know that there is a person John who works for O which is an office in Boston B.

(4)
$$person(J)$$
, $work-for(J, O)$, $office(O)$, $in(O, B)$, $Boston(B)$

We also know that work-for is a possible coercion relation,

$$(5) \quad (\forall x, y) work - for(x, y) \supset rel(x, y)$$

and that in is a possible implicit relation in compound nominals,

(6)
$$(\forall y, z) in(y, z) \supset nn(z, y)$$

Then the proof of all but the first conjunct of (3) is straightforward, by backchaining on axioms (5) and (6) into the ground instances of (4). We thus assume $(\exists e)call'(e, J)$, which constitutes the new information in the sentence.

Notice now that all of our local pragmatics problems have been solved. "The Boston office" has been resolved to O. The implicit relation between Boston and the office has been determined to be the in relation. The metonymy has been resolved by coercing "The Boston office" into "John, who works for the Boston office."

This is of course a simple example, and the analysis has shown only the correct interpretation is *possible*. It is the function of the weighted abduction scheme, described in the next section, to choose this interpretation over other possibilities. A more detailed discussion of these issues and more complex examples and arguments are given in Hobbs et al. (1990).

The contrast between the abductive approach and earlier inference models can be described succinctly as follows. In the models proposed by Rieger (1974) and by Sperber and Wilson (1986) one forward-chains from the text and tries to maximize the implications. In the abductive model, one backchains from the text and tries to minimize the assumptions.

3.3 Weighted Abduction

Our scheme for weighted abduction (Stickel, 1988) has three features.

First, every conjunct in the logical form of the sentence is given an assumability cost, corresponding to the need for this conjunct to be proven if an adequate interpretation is to be achieved. Thus, conjuncts arising from definite noun phrases and selectional constraints have higher assumability costs than those arising from indefinite noun phrases and main verbs.

Second, this cost is passed back to the antecedents in Horn clauses by a system of weights. Axioms are stated in the form

(7)
$$P_1^{w_1} \wedge P_2^{w_2} \supset Q$$

This says that P_1 and P_2 imply Q, but also that if the cost of assuming Q is c, then the cost of assuming P_1 is w_1c , and the cost of assuming P_2 is w_2c . (Stickel (1988) generalizes this to arbitrary functions of c.)

Third, factoring or synthesis is allowed. That is, goal expressions may be unified, in which case the resulting expression is given the smaller of the costs of the input expressions. This feature leads to minimality through the exploitation of redundancy.

In rules like (7), we generally assign the weights so that $w_1 + w_2 > 1$. Thus, less specific assumptions (Q) are favored over more specific ones $(P_1 \wedge P_2)$. But in

$$P_1^{.6} \wedge P_2^{.6} \supset Q$$

if P_1 has already been proved, it is cheaper to assume P_2 (for .6c) than to assume Q (for c). P_1 has provided evidence for Q, and assuming the "balance" P_2 of the necessary evidence for Q should be cheaper.

Factoring can also override less specific abduction. Suppose we have the axioms

$$P_1^{.6} \wedge P_2^{.6} \supset Q_1$$

 $P_2^{.6} \wedge P_3^{.6} \supset Q_2$

and we wish to derive $Q_1 \wedge Q_2$, where each conjunct has an assumability cost of \$10. Assuming $Q_1 \wedge Q_2$ will then cost \$20, whereas assuming $P_1 \wedge P_2 \wedge P_3$ will cost only \$18, since the two instances of P_2 obtained by backchaining can be unified.

Thus, the abduction scheme allows us to adopt the careful policy of favoring less specific abduction while also allowing us to exploit the redundancy of texts for more specific interpretations.

Exactly how the weights and costs should be assigned is a matter of continuing research. It is discussed further in Hobbs et al. (1990). In the remainder of this paper, this issue will be ignored. Our concern will rather be to show that the correct interpretations of metaphors are *possible* in the abductive approach.

In the current TACITUS implementation, whenever an assumption is made, it is checked for consistency. The extension of the abductive approach to metaphor interpretation suggests that this check should be soft rather than hard. Inconsistent assumptions should be allowed if they will result in an otherwise very good interpretation. This is the topic of Section 5.

It might seem that since we use only backchaining to find a proof and a set of assumptions, we cannot use superset information. However, the fact that we can make assumptions enables us to turn axioms around. In general, an axiom of the form

species ⊃ genus

can be converted into a biconditional axiom of the form

genus ∧ differentiae ≡ species

Often we will not be able to prove the differentiae, and in many cases we cannot even spell them out. But in our abductive scheme, this does not matter; they can simply be assumed. In fact, we need not state them explicitly at all. We can simply introduce a predicate that stands for all the remaining properties. It will never be provable, but it will be assumable. Thus, in addition to having axioms like that referred to in Section 4.3,

 $(\forall y)elephant(y) \supset clumsy(y)$

we may have axioms like

$$(\forall x) clumsy(y)^{.4} \land etc_1(y)^{.8} \supset elephant(y)$$

where the weights are distributed roughly according to the "semantic contribution" of each conjunct in the antecedent to the consequent.³ Then, even though we are strictly backchaining in search for an explanation, the fact that something is clumsy can still be used as (perhaps weak) evidence for its being an elephant, since we can assume the "et cetera" predication $etc_1(x)$ for a certain cost.

This device may seem ad hoc, especially in this paper since it is used in only two axioms where it is essential to get the correct interpretation to go through. On the contrary, however, we view the device as implementing a fairly general solution to the problems of nonmonotonicity in commonsense reasoning and vagueness of meaning in natural language, very similar to the use of abnormality predicates in circumscriptive logic (McCarthy, 1987). Whereas, in circumscriptive logic, one typically specificies a partial ordering of abnormality predicates in accordance with which they are minimized, in the weighted abduction framework, one uses a somewhat more flexible system of costs.

³Hobbs et al. (1990) addresses the issue of what "semantic contribution" means in probabilistic terms.

There is no particular difficulty in specifying a semantics for the "et cetera" predicates. Formally, etc_1 in the axiom above can be taken to denote the set of all things that are either not clumsy or are clumsy elephants. Intuitively, etc_1 conveys all the information one would need to know beyond clumsiness to conclude something is an elephant. As with nearly every predicate in an axiomatization of commonsense knowledge, it is hopeless to spell out necessary and sufficient conditions for an "et cetera" predicate. In fact, the use of such predicates in general is due largely to a recognition of this fact about commonsense knowledge.

The "et cetera" predicates could be used as the abnormality predicates are in circumscriptive logic, with separate axioms spelling out conditions under which they would hold. However, in the view adopted here, more detailed conditions would be spelled out by expanding axioms of the form

$$(\forall x)p_1(x) \wedge etc_1(x) \supset q(x)$$

to axioms of the form

$$(\forall x)p_1(x) \wedge p_2(x) \wedge etc_1(x) \supset q(x)$$

An "et cetera" predicate would appear only in the antecedent of a single axiom and never in a consequent. Thus, the "et cetera" predications are only place-holders for assumption costs. They are never proved. They are only assumed.

They constitute one of the principal devices for giving our logic "soft corners". We would expect them to pervade the knowledge base. Virtually any time there is an axiom relating a species to a genus, there should be a corresponding axiom, incorporating an "et cetera" predication, expressing the inverse relation.

3.4 The Integrated Framework

The idea of interpretation as abduction can be combined with the older idea of parsing as deduction (Kowalski, 1980, pp. 52-53; Pereira and Warren, 1983). Consider a grammar written in Prolog style just big enough to handle sentence (2).

(7)
$$(\forall i, j, k) np(i, j) \land v(j, k) \supset s(i, k)$$

(8)
$$(\forall i, j, k, l) det(i, j) \land n(j, k) \land n(k, l) \supset np(i, l)$$

That is, if we have a noun phrase from "inter-word point" i to point j and a verb from j to k, then we have a sentence from i to k, and similarly for rule (8).

We can integrate this with our abductive framework by moving the various pieces of expression (3) into these rules for syntax, as follows:

(9)
$$(\forall i, j, k, e, x, y, p) n p(i, j, y) \land v(j, k, p) \land p'(e, x)$$

 $\land Req(p, x) \land rel(x, y) \supset s(i, k, e)$

That is, if we have a noun phrase from i to j referring to y and a verb from j to k denoting predicate p, if there is an eventuality e which is the condition of p being true of some entity x (corresponding to call'(e,x) in (3)), if x satisfies the selectional requirement p imposes on its argument (corresponding to person(x)), and if x is somehow related to, or coercible from, y, then there is an interpretable sentence from i to k describing eventuality e.

(10)
$$(\forall i, j, k, l) det(i, j, the) \land n(j, k, w_1) \land n(k, l, w_2)$$

 $\land w_1(z) \land w_2(y) \land nn(z, y) \supset np(i, l, y)$

That is, if there is the determiner "the" from i to j, a noun from j to k denoting predicate w_1 , and another noun from k to l denoting predicate w_2 , if there is a z that w_1 is true of and a y that w_2 is true of, and if there is an nn relation between z and y, then there is an interpretable noun phrase from i to l denoting y.

These rules incorporate the syntax in the literals like v(j, k, p), the pragmatics in the literals like p'(e, x), and the compositional semantics in the way in which the pragmatics literals are constructed out of the information provided by the syntax literals.

To parse with a grammar in the Prolog style, we prove s(0, N) where N is the number of words in the sentence. To parse and interpret in the integrated framework, we prove $(\exists e)s(0, N, e)$.

One of the appeals of declarative formalisms is that they can be used equally for interpretation and generation. This is true of our framework as well. To generate a sentence describing a given eventuality is to prove $(\exists n)s(0,n,E)$. In generation, it is the terminal nodes in the grammar, atoms like det(i,j,the), that are assumed. Thus, in generation, assumptions correspond to actions.

This approach can be extended upward to include the recognition of coherence relations in discourse and downward to include the spellings or pronunciations of words (Hobbs et al., 1990).

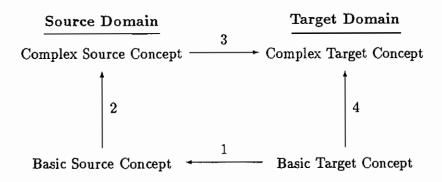


Figure 1: Analogical Processes Underlying Metaphor.

The integrated approach suggests a shift of perspective. Initially, the problem of interpretation was viewed as being given certain observable facts, namely, the logical form of the sentence, and finding a proof that demonstrates why they are true. In this section, we no longer set out to prove the observable facts. Rather we set out to prove that we are viewing a coherent situation; it is built into the rules specifying what situations are coherent that an explanation must be found for the observable facts.

4 Interpreting Metaphors by Abduction

4.1 The Schema for Metaphor

The basic schema for metaphor (and analogy) is that shown in Figure 1.

There are two domains of knowledge, a source domain that is generally very well understood, expressed as a highly elaborated set of axioms, and a target domain, that is generally less well understood.⁴ We wish to reason or describe something in the target domain. Rather than doing so directly, we map a basic concept in the target domain into a corresponding basic concept in the source domain. We reason or describe in the source domain, with its richer vocabulary and set of axioms, yielding a complex concept in the source domain. Then we map the result back into the target domain, thereby expressing a complex concept there.

⁴The term "domain" carries no theoretical weight in this framework. It is just a way of speaking about a group of axioms intuitively perceived to be about the same topic.

Interpreting a metaphor is a matter of reversing this process. We are given a complex concept in the target domain, expressed in the vocabulary of the source domain. The problem is to discover what this expression means by determining how it is composed out of basic concepts in the target domain. To do this, we decompose the complex concept into basic concepts in the source domain, and then undo the analogical mapping to determine the meaning in the target domain.

A computational account of metaphor must specify precisely how each of the arrows in this commuting diagram is realized in a formal system. Our answer is essentially as follows. The relation between domains is taken to be simply identity. Predicates from the source domain will simply be predicated of entities from the target domain. This of course brings with it problems of logical consistency, and how to deal with that is the subject of Section 5. The relations between basic and complex concepts will be those implicational relations encoded in the axioms. Interpreting a metaphor by abduction will then be a matter of backchaining along arrows 3, 2, and 1 to an account in terms of the basic concepts in the target domain.

We show how this works for three examples, a conventionalized metaphor schema, a standard category metaphor whose interpretation depends on context, and a novel metaphor. That these three kinds of cases can be handled in the abductive approach ought to be suggestive of the power of the approach in general.

4.2 A Conventionalized Metaphor Schema

The first metaphor to be examined is

(11) The variable N goes from 1 to 100.

Here, the target domain, computer science, is being modeled in terms of the domain of spatial or perhaps more abstract topological relations. This metaphor rests on the core metaphor that identifies a variable having a value with an entity being located at some place. This conventionalized identification can be expressed by the following axiom:⁵

(12)
$$(\forall e, x, y) variable(x) \land value'(e, y, x) \supset at'(e, x, y)$$

That is, if x is a variable and e is the condition of y's being its value, then e is also the condition of x being at y. The predicate at is thus not merely

⁵In fact, the existence of such an axiom in the knowledge base is precisely what it means in this framework for the metaphor to be conventional.

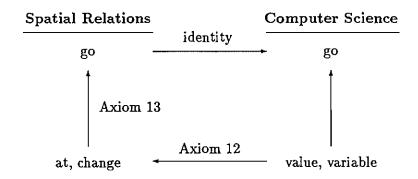


Figure 2: Inference Processes in a Conventionalized Metaphor Schema.

a spatial term but more generally a topological relation locating a figure against a ground.

The relation between the complex predicate go and more basic predicates is expressed by the following axiom, capturing the fact that a change in location is a going event:

(13)
$$(\forall e, e_1, e_2, x, y, z) change'(e, e_1, e_2) \land at'(e_1, x, y) \land at'(e_2, x, z)$$

 $\supset go'(e, x, y, z)$

That is, if e is a change from state e_1 to state e_2 where e_1 is the state of x being at y and e_2 is the state of x being at z, then e is a going by x from y to z.

Now consider the example. Its logical form is

$$(\exists e_0)go'(e_0, N, 1, 100) \land variable(N)$$

This is a statement in the target domain, computer science. But we treat it as though it were a statement in the source domain and use source domain axiom (13) to decompose the complex concept go into the more basic concepts of change and at. We then use axiom (12) to interpret the at relation. The two atoms variable(N) generated in this way are unified with the identical atom from the logical form, and that condition, the change, and the two value relations are assumed, yielding the minimal interpretation. We thereby have interpreted sentence (11) as asserting a change in value for the variable N. This process is illustrated in Figure 2.

4.3 A Category Metaphor

The next metaphor to be examined is

(14) John is an elephant.

A number of suggestions have been made about the appropriate inferences to draw in cases such as this. Ortony et al. (1978) said that it is high salience properties that should be transferred, such as size in the case of elephants. Glucksberg and Keysar (1990) say it is diagnostic properties; that is, in (14), we look for some property of elephants for which an elephant is the prototypical exemplar, such as large size. Carbonell (1982) has argued that abstract properties, rather than physical properties, should be transferred; thus, "has a trunk" should not be transferred. Gentner (1983) has argued that relations (predicates with two or more arguments) are more frequently transferred than monadic properties.

One difficulty with all these suggestions is that they do not depend on context, whereas we know that interpretation always depends on context. Consider the following sentence:

(15) Mary is graceful, but John is an elephant.

The most reasonable interpretation is that John is clumsy. This is not an especially high salience property of elephants. It is not clear that elephants are prototypical exemplars of clumsiness. Clumsiness seems to be intermediate between an abstract and a physical property. And it is not a relation.

The non-abductive analysis of this example was relatively clean in Hobbs (1983). There was an axiom that said elephants are clumsy:⁶

$$(\forall y)elephant(y) \supset clumsy(y)$$

That inference was selected because it led to the recognition of a contrast relationship between the two clauses, as signalled by the conjunction "but".

In the abductive approach, the analysis is complicated somewhat by the fact that we can only backchain. This axiom must be rewritten as

$$(16) \quad (\forall y) clumsy(y) \land etc_2(y) \supset elephant(y)$$

⁶Elephants of course are not clumsy, but according to our conventional stereotype, they are. This property is therefore in our "knowledge" base and hence available in metaphor interpretation. Searle (1979) made this point, with respect to gorillas' being "fierce, nasty, prone to violence, and so forth."

That is, if something is clumsy and some other unspecified properties hold, then it is an elephant.

We will need to introduce a further complication as well, since we will have to refer explicitly to the properties of clumsiness, elephanthood, and grace. Axiom (16) must be rewritten as follows:

(17)
$$(\forall e_3, y) clumsy'(e_3, y) \land etc_2(e_3, y)$$

 $\supset (\exists e_2) elephant'(e_2, y) \land gen(e_3, e_2)$

That is, if e_3 is the condition of y's being clumsy and some other unspecified things are true of e_3 and y, then there is a condition e_2 of y's being an elephant. Furthermore, there is a very tight relation between e_3 and e_2 : y is an elephant by virtue of its being clumsy and the other things being true. We encode this relation with the predicate gen, since it is similar to the "generates" relation common in the philosophical literature.

In Hobbs (1983) the interpretation of (15) was driven by the recognition of a coherence relation between the clauses. In many cases in the abductive approach, especially where a conjunction occurs explicitly, this can be subsumed under the general characterization of interpretation. In (15), the "but" relation is part of the information conveyed by the text, and consequently part of what needs to be explained.⁸ We can say that a "but" relation holds between two eventualities e_1 and e_2 if they are contradictory properties p and p of two entities p and p that are similar by virtue of sharing some other property p:

$$(\forall p, q, x, y, e_1, e_2, e_4) p'(e_1, x) \land not'(e_2, e_4) \land p'(e_4, y) \land q(x) \land q(y) \supset but(e_1, e_2)$$

This however is too strong. It may be that the contrast is between not e_1 and e_2 but between eventualities related to e_1 and e_2 . In the case of example

Mary is graceful; John is an elephant.

This is because the mere adjacency of the clauses conveys information—namely, that the two situations are somehow related. One possible relation is contrast, which is characterized roughly as "but" is. But other relations are theoretically possible as well, leading to the sense we have that it is less certain that the interpretation of the second clause is "John is clumsy". The next clause might be "Mary can dance on his back," in which case the second clause would not be in contrast with the first but background for the third, and John would be a real rather than a metaphorical elephant.

⁷The analyses of a large number of phenomena in discourse require an appeal to this "generates" relation between eventualities.

⁸The same interpretation is available for the sentence

(15), the contrast is between e_1 and an eventuality related to e_2 , so for this example we will rewrite the above axiom as follows:

(18)
$$(\forall p, q, x, y, e_1, e_2, e_3, e_4)p'(e_1, x) \land not'(e_3, e_4) \land p'(e_4, y)$$

 $\land gen(e_3, e_2) \land q(x) \land q(y) \supset but(e_1, e_2)$

That is, a "but" relation holds between e_1 and e_2 if there is a p such that e_1 is p's being true of some x, and there is an e_3 that generates e_2 that is the negation of an e_4 which is p's being true of some y, and there is some q true of x and y. (This axiom is second-order, but not seriously so, if we restrict the instantiations of the predicate variables to predicate constants.)

Next we need an axiom relating clumsiness and grace.

(19)
$$(\forall e_3, e_4, y) not'(e_3, e_4) \land graceful'(e_4, y) \supset clumsy'(e_3, y)$$

That is, if e_3 is the condition of e_4 not being true, where e_4 is the condition of y's being graceful, then e_3 is the condition of y's being clumsy.

Suppose we also know that Mary and John are people:

Now we are ready to interpret sentence (15). Its logical form is

$$(\exists e_1, e_2)$$
graceful' $(e_1, M) \land elephant'(e_2, J) \land but(e_1, e_2)$

We can then backchain on axiom (17) from "elephant" to "clumsy", assume $etc_2(e_3, J)$, backchain on axiom (19) from "clumsy" to "not graceful", and assume $not'(e_3, e_4)$ and $graceful'(e_4, J)$. We also assume $graceful'(e_1, M)$. Then we have a proof of $but(e_1, e_2)$, using axiom (18), with p instantiated to graceful and q instantiated to person.

We have thereby interpreted the metaphor. Figure 3 illustrates the interpretation of "elephant", although it was the requirement to explain the "but" relation that drove the interpretation.

This account is somewhat more complex than that given in Hobbs (1983), but every complication is independently motivated. By subsuming metaphor interpretation under a general account of interpretation, we more than justify the moderate increase in complexity.

4.4 A Novel Metaphor

The last metaphor to be examined occurred in *Newsweek* in a quote by an American Congressman complaining that the bills the Congress passes are too easy for the President to veto.

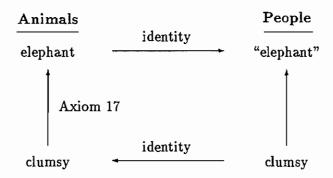


Figure 3: Inference Processes in a Category Metaphor.

(20) We insist on serving up these veto pitches that come over the plate the size of a pumpkin.

This metaphor evokes a mapping between a schema for the passage of a bill into law by the American government and a schema for baseball. The Congress schema says that Congress sends a bill to the President, and then the President signs or vetoes it. The baseball schema says that the pitcher sends a ball to the batter, and then the hitter either hits or misses it or hits a foul ball. The mapping identifies the Congress with the pitcher, the President with the batter, and the bill with the ball. Vetoing the bill corresponds to hitting the ball.

To clarify the exposition of this example, variables in axioms and the logical form that will be unified in the final proof will be represented with the same letter, differently subscripted. Unsubscripted variables and the subscripts 0 and 1 will be used in the logical form. The subscript 2 is used in axiom (21), 3 in axiom (22), and 4 in axiom (23). Thus, x is Congress in the logical form, x_2 is Congress in axiom (21), x_3 is the pitcher in axiom (22), and x_4 is the sender/pitcher in axiom(23).

A diagram of the proof is presented in Figure 4.

In the abductive framework, a schema is represented as an axiom that has in the antecedent a "schema predication", with all of the role fillers as arguments, and in the consequent the various properties of the role fillers. A schema is often used in the interpretation of a text because assuming the single schema predication explains so much of the content of the text; it is one way of arriving at a minimal abductive proof. Several different schemas

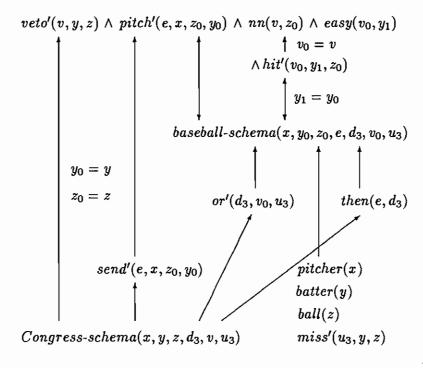


Figure 4: Abductive Proof for Novel Metaphor.

can be used simultaneously by simply assuming or proving their schema predications, with their variables instantiated in the appropriate ways.

The Congress schema would thus be encoded in the following axiom:

(21)
$$(\forall z_1, e_1, d_1, v_1, u_1) Congress-schema(x_2, y_2, z_2, e_2, d_2, v_2, u_2)$$

 $\equiv Congress(x_2) \land President(y_2) \land bill(z_2)$
 $\land send'(e_2, x_2, z_2, y_2) \land or'(d_2, v_2, u_2) \land veto'(v_2, y_2, z_2)$
 $\land sign'(u_2, y_2, z_2) \land then(e_2, d_2)$

That is, there is a Congress schema situation involving the listed variables, if and only if x_2 is Congress, y_2 is the President, z_2 is a bill, e_2 is a sending by Congress of the bill to the President, d_2 is the disjunction of the vetoing v_2 by the President of the bill and the signing u_2 by the President of the bill, and d_2 happens after e_2 .

The baseball schema would be encoded in the following axiom:

(22)
$$(\forall x_3, y_3, z_3, e_3, d_3, v_3, u_3)$$
baseball-schema $(x_3, y_3, z_3, e_3, d_3, v_3, u_3)$
 $\equiv pitcher(x_3) \land batter(y_3) \land ball(z_3)$
 $\land pitch'(e_3, x_3, z_3, y_3) \land or'(d_3, v_3, u_3) \land hit'(v_3, y_3, z_3)$
 $\land miss'(u_3, y_3, z_3) \land then(e_3, d_3)$

That is, there is a baseball schema situation involving the listed variables, if and only if x_3 is the pitcher, y_3 is the batter, z_3 is the ball, e_3 is a pitching by the pitcher of the ball to the batter, d_3 is the disjunction of the hitting v_3 by the batter of the ball and the missing u_3 by the batter of the ball, and d_3 happens after e_3 .

Both schema axioms have been written as biconditionals, but only axiom (22) will be used in both directions in this example.

One further axiom is required, relating sending and pitching.

(23)
$$(\forall e_3, x_3, y_3, z_3)$$
 send' $(e_3, x_3, z_3, y_3) \land etc_3(e_3, x_3, y_3, z_3)$
 $\supset pitch'(e_3, x_3, z_3, y_3)$

That is, if e_3 is a sending by x_3 of z_3 to y_3 and some other unspecified conditions hold for these entities, then e_3 is a pitching by x_3 of z_3 to y_3 .

To focus on the metaphor, we will simplify the example somewhat. We assume that "that come over the plate the size of a pumpkin" has already been interpreted to mean "that are easy to hit". We will also assume that "we" has been resolved to Congress and that we therefore know

Congress(x). We assume that the fact that the control verb "serving up" is applied to "pitches" has enabled us to determine that it is Congress that is pitching. Then the logical form of the portion of the sentence that concerns us would be as follows, where all the variables are existentially quantified:

$$\dots \wedge veto'(v, y, z) \wedge pitch'(e, x, z_0, y_0) \wedge nn(v, z_0) \wedge easy(v_0, y_1) \wedge hit'(v_0, y_1, z_0) \wedge \dots$$

That is, there is a vetoing event v by someone y of something z, there is a pitching event e by Congress x of something z_0 to someone y_0 , the vetoing v is related somehow (nn) to the thing z_0 that is pitched, and the hitting v_0 by someone y_1 of z_0 is easy for y_1 .

This expression needs to be proved abductively. The conjuncts $pitch'(e, x, z_0, y_0)$ and $hit'(v_0, y_1, z_0)$ can be proved by assuming the baseball schema, instantiated as follows:

```
baseball-schema(x, y_0, z_0, e, d_3, v_0, u_3)
```

so that y_0 and y_1 (the one to whom something is pitched and the one who finds it easy to hit) are identified.

But now the baseball schema axiom can be used in the opposite direction, to backchain into the following predications:

$$pitch'(e, x, z_0, y_0), or'(d_3, v_0, u_3), then(e, d_3)$$

By assuming the "et cetera" predication of axiom (23), we can backchain from the first of these into

$$send'(e, x, zy_4)$$

But now if we assume the remaining conjuncts on the right-hand side of axiom (22),

$$pitcher(x), batter(y_0), ball(z_0), miss'(u_3, y_0, z_0)$$

then we can prove the baseball schema from the Congress schema, instantiated as follows:

```
Congress-schema(x, y_0, z_0, e, d_3, v_0, u_3)
```

Thus, Congress is identified as a pitcher, the President as a batter, and so forth.

We can prove veto'(v, y, z) in the logical form from this instantiation of the Congress schema, yielding

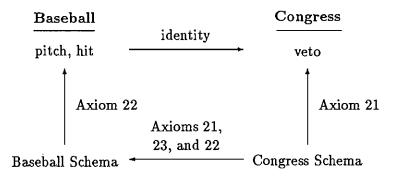


Figure 5: Inference Processes in a Novel Metaphor.

 $Congress-schema(x, y, z, e, d_3, v, u_3)$

so that the implicit agent y of the vetoing gets identified with the President/batter y_1 , the vetoing v gets identified with the hitting v_0 , and the thing vetoed z is identified with the thing pitched z_0 .

Finally, nn(v, z) must be instantiated to some relationship between the vetoing v and the thing pitched z, and either veto'(v, y, z) or hit'(v, y, z) will do. In fact, maximum redundancy is achieved by assuming these two relations are the same, and this is one reason the vetoing and hitting are identified, rather than the vetoing and the missing.

Thus, by assuming the Congress schema, assuming what was needed to infer a pitching from a sending, and assuming the missing pieces of the baseball schema, we derived the baseball schema and identified the corresponding actions, thereby interpreting the novel metaphor. The two schemas together then accounted for the propositional content of the sentence.

This is illustrated in Figure 5. We assume the Congress Schema, and this allows us, via axiom (21), to explain "veto". Axioms (21), (23), and (22), the last used from right to left, establish the baseball schema, from which we can infer "pitch" and "hit", by axiom (22) used from left to right. This results in the identification of the hitting and the vetoing.

5 Metaphor and Truth

There is a problem in our account of how examples (15) and (20) are interpreted. They require the assumption of propositions that are not true.

John is not an elephant, and the bill is not a ball. Here I will sketch two possible solutions to this problem.

1. Predicate Coercion: When a predicate is applied to an argument for which it is not appropriate, there are two possible interpretive moves. We can decide that the argument actually refers to something other than it denotes explicitly—we can coerce the argument into something related to it. This is metonymy. Or we can decide that the predicate actually denotes a property other than the one it denotes explicitly—we can coerce the predicate to a related predicate. Metaphor is one example of this. Thus, we are likely to interpret

Dan Quayle couldn't read Plato.

metonymically. We coerce from Plato to the dialogues written by Plato. By contrast, we are likely to interpret

George Bush couldn't read Saddam Hussein.

metaphorically. We coerce the predicate, taking "read" to mean "understand". In metonymy, one applies a coercion function k to the argument, transforming p(x) into p(k(x)), in order to achieve congruence between the predicate and the argument. In our functionless notation, this becomes

$$p(y) \, \wedge \, Req(p,y) \, \wedge \, rel(y,x)$$

where Req(p, y) is the requirement that p imposes on its argument, and rel(y, x) expresses the coercion relation between y and x.

By analogy, this would suggest that metaphor be handled by applying a coercion function to the predicate, transforming p(x) into k(p)(x). In our functionless notation, this becomes

$$q(x) \wedge Req(q,x) \wedge Rel(q,p)$$

The predicate q would be new. The question arises as to what q means. The meaning—even the denotation—of a predicate is determined or at least constrained by the axioms it occurs in. To construct a new predicate q we would have to specify the axioms in which it occurs. In abductive interpretation, a subset of the axioms involving p are selected as relevant to the

⁹Example(11) does not run into this problem only because at has already by convention been abstracted into a topological relation more general than simple spatial location.

¹⁰A process of predicate coercion is also proposed by Nunberg (1991) and by Bobrow et al. (1991) for different but compatible purposes.

sentence, i.e., those that lead to the best explanation of the content of the sentence. If we substitute q for p in just these axioms, we have thereby specified the axioms for q and hence delimited its meaning. We are in effect achieving what selective inferencing did in Hobbs (1983). The uncertainties in this process correspond to the uncertainties we sometimes experience in interpreting metaphors; they are one of the sources of the metaphor's power.

In this approach *elephant*, in the context of example (15), is coerced into another predicate, which is implicationally related to *clumsy* and perhaps to *large*, but does not imply the existence of a trunk.

2. Interpretation and Judgment: In the abductive approach to interpretation, we make assumptions when we are unable to prove something (for less cost). But these assumptions can play a number of different roles. In Section 3.2 and in many cases in Section 4, assumptions are used to accept new information. More generally, however, they can be used to accommodate speakers, whatever they say. Suppose someone says,

John called Mary a Marxist, and she insulted him too.

To interpret this sentence, we must assume that it is bad to be a Marxist, or at least that the speaker believes it, even though we may not believe it ourselves. But we will not normally change our beliefs as a result of interpreting this sentence.

One can also use assumptions to interpret one's way past a mistake. Suppose the approach of Section 3.4 were carried all the way down to the level of individual letters. We would have the following rule to tell us how the pronoun "it" is spelled:

$$(\forall i, j, k)I(i, j) \land T(j, k) \supset pro(i, k, it)$$

That is, if there is the letter "i" between point i and point j and the letter "t" between point j and point k, then there is the pronoun "it" between point i and point k. If we then encountered the string

If is easy to please John.

we could interpret it by assuming that the second letter is in fact a "t" and not an "f". This may yield the best interpretation of the entire set of observables in the text, even though it is flatly contradicted by one of the observables.

Assumptions can also be used for adopting and using local conventions. Consider the following exchange (due to John DuBois.)

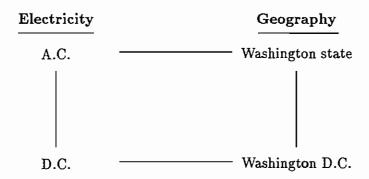


Figure 6: Cognitive Processes in a Local Convention.

A: I'm going to Washington tomorrow.

B: D.C. or A.C.?

A: A.C.

In this dialogue "A.C." has come to mean "state", and assuming this equivalence is necessary for interpreting it, as illustrated in Figure 6. But that does not mean this identification will persist to other dialogues.

Finally, in an approach to generation presented in Hobbs et al. (1990) based on the integration described in Section 3.4, assumptions correspond to actions, namely, the uttering of words.

We have said that to interpret a text is to find the best explanation for why it would be true, not why it is true. Deciding whether something is true is a logically (though not necessarily chronologically) separate process, one that we can call judgment.

We can take metaphor interpretation as working in much the same way. We make certain assumptions in order to interpret the metaphor, such as that John is an elephant and that the bill is a ball, and then in a logically separate judgement step, we decide which of our assumptions we are in fact prepared to believe.

Let us carry this approach one more step both toward formalization and toward embedding it in a larger framework. In Hobbs et al. (1990), it is suggested that a rational agent can be seen as going through the world, continuously trying to prove abductively the proposition "The situation I am in is coherent and I will thrive in it". The first clause generates in-

¹¹Actually, one could see the first clause as a precondition for the second.

terpretation, the second action. One kind of coherent situation, involving both interpretation and action is a turn in a conversation. Here there is a speaker S, a hearer H, and an utterance u. The utterance is an action on the part of S that serves in the achievement of S's goals. The utterance has an interpretation ϕ , which we may think of as a set of propositions. The hearer makes some kind of judgment about the information contained in ϕ . This can all be expressed by the rule

$$(\forall u, \phi, H, S) Serve-Goal(u, S) \land Interp(u, \phi) \land Judge(H, \phi) \\ \supset Turn-in-Conversation(u, S, H)$$

That is, if an utterance u serves a goal of the speaker S, the interpretation of u is ϕ , and the hearer H judges ϕ , then there is a turn in a conversation in which S utters u to H.

A small set of axioms enable backchaining from $Interp(u, \phi)$ into the whole abductive framework of interpretation described in this paper, via a "grammar" of the sort described in Section 3.4. One may think of this as the entry into the *informational* aspect of discourse.

Other axioms having Serve-Goal(u, S) as their consequent would tap into the whole *intentional* aspect of discourse, as elucidated in the work of Cohen and Perrault (1979) and many others. Thus, there might be an axiom that says that if H's believing ϕ serves a goal of S, then u serves a goal of S.

Because the conjuncts $Interp(u, \phi)$ and Serve-Goal(u, S) share variables, the informational and intentional aspects can influence each other. Thus, what might otherwise be the best interpretation of an utterance could be rejected if there is no way to relate it to the speaker's goals.

Finally, a first cut at an expansion of $Judge(H, \phi)$ might go as follows. To judge ϕ one must judge each proposition P in ϕ . There are three possibilities for P. P may already be mutually known, the given, in which case there is nothing to do. P may be inconsistent with what is already known, in which case it is judged false and rejected. Otherwise, P will be entered into the knowledge base, as mutual knowledge. This of course is oversimplified. In fact, the conjunct $Judge(H, \phi)$ taps into the whole domain of belief revision.

In this account, it would be perfectly normal in the course of interpretation to assume a proposition that is known to be false. The judgment as to whether it should become a permanent belief is part of a logically separate step.

The predicate coercion solution to the problem of metaphor and truth has the advantage of giving an analogous treatment to metaphor and metonymy. Its disadvantage is that it involves a significant increase in notational complexity. The judgment solution has the advantage of requiring nothing that is not already required in a larger framework for discourse interpretation and generation, but of course means that the details of that framework must be worked out.

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